

24 November 2010

1. (5p)	2. (6p)	3. (9p)	4.(4p)	5. (6p)	6. (6p)	Th. (4p)	Σ (Max 40p)

Corrected by:

1. Let be given the matrices $A = \begin{pmatrix} 1 & 4 & 0 \\ 2 & 0 & 3 \end{pmatrix}$, $B = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ and $C = \begin{pmatrix} 2 & 1 \\ 1 & 0 \end{pmatrix}$

Find $2A$; $A*B$; $C*B$; $B+C$!

2. Find the following integrals: a.) $\int 3x^8 + \frac{5}{x^2 + 1} dx$; b.) $\int 3x^2 \cdot \ln x \, dx$;

3. Find the following integrals

$$\text{a.) } \int \frac{x-2}{x \cdot (x^2+1)} dx \quad ; \quad \text{b.) } \int_0^1 (x^7 + 5x - 2)^4 \cdot (7x^6 + 5) dx$$

4. Find the area between $f(x) = x^2$ and $g(x) = 2 - x$ over the interval $[0; 2]$!

5. Find the arc length of the function $f(x) = \frac{2}{3} \sqrt{(x+2)^3}$ over the interval $[1 ; 6]$!

6. Find the following improper integral: $\int_0^{\infty} \frac{2}{x^2 + 8x + 15} dx$

Theoretical question:

Show that the equation of the plane passing through the point $P_0 = (x_0, y_0, z_0)$ and perpendicular to the vector $\underline{n} = n_x \underline{i} + n_y \underline{j} + n_z \underline{k}$ is $n_x(x - x_0) + n_y(y - y_0) + n_z(z - z_0) = 0$